

※Single Choice (1~15, 5% each) (每題恰有一解, 答對得 5 分, 答錯或不答得 0 分)

1. Find the domain of the function $f(x) = \sqrt{1-x^2}$.

Select the correct answer.

- (A) (0,1) (B) [0,1] (C) (-1,1) (D) [-1,1] (E) none of above.

2. Find the range of the function $f(x) = \sqrt{1-x^2}$.

Select the correct answer.

- (A) (0,1) (B) [0,1] (C) (-1,1) (D) [-1,1] (E) none of above.

3. Find the limit, $\lim_{x \rightarrow \infty} \sin x = ?$

Select the correct answer.

- (A) 0 (B) 1 (C) -1 (D) ∞ (E) does not exist.

4. Find the limit, $\lim_{x \rightarrow 0} \frac{\sqrt{x^2+1}-1}{x^2} = ?$

Select the correct answer.

- (A) 0 (B) 1 (C) 2 (D) $\frac{1}{2}$ (E) does not exist.

5. Find the limit, $\lim_{x \rightarrow -\infty} \frac{x}{\sqrt{x^2+x}} = ?$

Select the correct answer.

- (A) 0 (B) 1 (C) -1 (D) 2 (E) none of above.

6. Let $f(x) = \begin{cases} 1, & x \geq 0 \\ -1, & x < 0 \end{cases}$. Find the limit, $\lim_{x \rightarrow 0} f(x) = ?$

Select the correct answer.

- (A) 0 (B) 1 (C) -1 (D) does not exist (E) none of above.

7. Let $f(x) = \begin{cases} 1, & x \geq 0 \\ -1, & x < 0 \end{cases}$. Find the point where $f(x)$ is not continuous.

Select the correct answer.

- (A) $x = 0$ (B) $x = 1$ (C) $x = -1$ (D) $x = 2$ (E) $x = -2$.

8.

$$\text{Let } f(x) = \begin{cases} 1 & , \quad x \leq -1 \\ ax + b & , \quad -1 < x < 3 \\ -1 & , \quad 3 \leq x \end{cases} . \text{ If } f(x) \text{ is continuous on } (-\infty, \infty), \text{ then } a + b = ?$$

Select the correct answer.

- (A) 1 (B) 2 (C) 3 (D) 4 (E) none of above.

9. If $f(x) = x^2 - 8x + 9$, then $f'(a) = ?$

Select the correct answer.

- (A) $x^2 - 8x + 9$ (B) $2x - 8$ (C) $a^2 - 8a + 9$ (D) $2a - 8$ (E) none of above.

10.

$$\text{Find } \frac{d}{dx}(x \sin x) = ?$$

Select the correct answer.

- (A) $\sin x$ (B) $\cos x$ (C) $x \sin x$ (D) $x \cos x$ (E) none of above.

11.

$$\text{Find } \frac{d}{dx} \left(\frac{\sin x}{x} \right) = ?$$

Select the correct answer.

- (A) $\frac{\cos x}{x}$ (B) $\frac{x \cos x - \sin x}{x^2}$ (C) $\frac{x \sin x - \cos x}{x^2}$ (D) $\frac{\cos x}{x^2}$ (E) none of above.

12.

$$\text{Find } \frac{d}{dx}(\sin(\sin x)) = ?$$

Select the correct answer.

- (A) $\cos(\cos x)$ (B) $\cos(\sin x)$ (C) $\sin x \cos(\sin x)$ (D) $\cos x \cos(\sin x)$
(E) none of above.

13.

$$\text{Find } \int_0^{2\pi} \sin x \, dx = ?$$

Select the correct answer.

- (A) 0 (B) 1 (C) 2 (D) 4 (E) none of above.

14.

$$\text{Find } \int_0^{2\pi} |\sin x| \, dx = ?$$

Select the correct answer.

- (A) 0 (B) 1 (C) 2 (D) 4 (E) none of above.

15. Find $\int_0^{\infty} \sin x \, dx = ?$

Select the correct answer.

- (A) 0 (B) 1 (C) 2 (D) 4 (E) none of above.

※Multiple Choice(16~20, 5% each)(每題至少有二正確選項, 完全答對得5分, 其餘情形得0分)

16. Let $f(x) > 0$ and $g(x) > 0$ for $x \in \mathbb{R}$.

Select the correct statements.

- (A) $f(x) + g(x) > 0$ for $x \in \mathbb{R}$.
(B) $f(x) - g(x) > 0$ for $x \in \mathbb{R}$.
(C) $f(x)g(x) > 0$ for $x \in \mathbb{R}$.
(D) $\frac{f(x)}{g(x)} > 0$ for $x \in \mathbb{R}$.
(E) $f(g(x)) > 0$ for $x \in \mathbb{R}$.

17. Let $f(x)$ and $g(x)$ be two continuous functions on \mathbb{R} .

Select the correct statements.

- (A) $f(x) + g(x)$ is continuous on \mathbb{R} .
(B) $f(x) - g(x)$ is continuous on \mathbb{R} .
(C) $f(x)g(x)$ is continuous on \mathbb{R} .
(D) $\frac{f(x)}{g(x)}$ is continuous on \mathbb{R} .
(E) $f(g(x))$ is continuous on \mathbb{R} .

18. It is known that $\frac{d}{dx}(\ln x) = \frac{1}{x}$ for $x > 0$.

Select the correct statements.

- (A) $\frac{d}{dx}(\ln|x|) = \frac{1}{x}$ for $x < 0$.
(B) $\frac{d}{dx}(\ln|x|) = -\frac{1}{x}$ for $x < 0$.
(C) $\frac{d}{dx}(\ln(2x)) = \frac{1}{x}$ for $x > 0$.
(D) $\frac{d}{dx}(\ln(2x)) = \frac{1}{2x}$ for $x > 0$.
(E) $\int \frac{1}{x} \, dx = \ln|x| + C$

19. Let $f(x)$ and $g(x)$ be two integrable functions with $f(x) > g(x)$, $x \in \mathfrak{R}$.

Select the correct statements.

(A) $\int_1^2 f(x) + g(x) dx > 0$

(B) $\int_1^2 f(x) - g(x) dx > 0$

(C) $\int_1^2 f(x) g(x) dx > 0$

(D) $f^2(x) > g^2(x)$ for $x \in \mathfrak{R}$.

(E) $f^3(x) > g^3(x)$ for $x \in \mathfrak{R}$

20. Consider the function $f(x) = x e^{-x}$, $x \in \mathfrak{R}$.

Select the correct statements.

(A) $f(x)$ is continuous on \mathfrak{R} .

(B) $\lim_{x \rightarrow \infty} f(x) = 0$

(C) $\lim_{x \rightarrow -\infty} f(x) = \infty$

(D) $\frac{d}{dx}(x e^{-x}) = e^{-x} - x e^{-x}$

(E) $\int x e^{-x} dx = e^{-x} - x e^{-x} + C$.

ANSWER

1	2	3	4	5	6	7	8	9	10
D	B	E	D	C	D	A	C	D	E

11	12	13	14	15
B	D	A	D	E

16	17	18	19	20
A, C, D, E	A, B, C, E	A, C, E	B, E	A, B, D