

※Single Choice (1~15, 5% each) (每題恰有一解，答對得 5 分，答錯或不答得 0 分)

1. Find the domain of the function $f(x) = \ln x$.

Select the correct answer.

- (A). $(-\infty, \infty)$ (B). $(-\infty, 0)$ (C). $(-\infty, 0]$ (D). $(0, \infty)$ (E). $[0, \infty)$

2. Find the range of the function $f(x) = \ln x$.

Select the correct answer.

- (A). $(-\infty, \infty)$ (B). $(-\infty, 0)$ (C). $(-\infty, 0]$ (D). $(0, \infty)$ (E). $[0, \infty)$

3. $\lim_{x \rightarrow 0} \frac{\sqrt{x+1} - 1}{x} = ?$

Select the correct answer.

- (A). 0 (B). 1 (C). 2 (D). 0.5 (E). none of above

4. If $\lim_{x \rightarrow 0} \frac{\sin x}{x} = 1$, find the value of $\lim_{x \rightarrow 0} \frac{\sin(3x)}{x}$.

Select the correct answer.

- (A). 0 (B). 1 (C). 3 (D). $\frac{1}{3}$ (E). none of above

5. $\lim_{x \rightarrow 0} \frac{\sin^2 3x}{x^2} = ?$

Select the correct answer.

- (A). 0 (B). 1 (C). 3 (D). $\frac{1}{3}$ (E). none of above

6. Which of the following statement is the $\varepsilon - \delta$ definition of $\lim_{x \rightarrow a} f(x) = L$?

Select the correct answer.

- (A). For every $\varepsilon > 0$, there is a $\delta > 0$ such that $|f(x) - L| < \varepsilon$ whenever $|x - a| < \delta$.
- (B). For every $\varepsilon > 0$, there is a $\delta > 0$ such that $|f(x) - L| < \delta$ whenever $0 < |x - a| < \varepsilon$.
- (C). For every $\varepsilon > 0$, there is a $\delta > 0$ such that $|f(x) - L| < \varepsilon$ whenever $0 < |x - a| < \delta$.

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(D). For every $\varepsilon > 0$, there is a $\delta > 0$ such that $|f(x) - L| < \delta$ whenever $|x - a| < \varepsilon$.

(E). none of above

7. Let $f(x) = \begin{cases} 1 & , x \leq 0 \\ ax + b & , 0 < x < 1 \\ 2 & , 1 \leq x \end{cases}$. If $f(x)$ is continuous on $(-\infty, \infty)$, then $a - b = ?$

Select the correct answer.

- (A). 0 (B). 1 (C). 2 (D). 3 (E). none of above

8. $\frac{d}{dx} \sin(x^3) = ?$

Select the correct answer.

- (A). $\cos(3x^2)$ (B). $3x^2 \cos(x^3)$ (C). $3 \sin^2 x$ (D). $\sin(3x^2)$ (E). none of above

9. $\frac{d}{dx} \sin^3 x = ?$

Select the correct answer.

- (A). $\cos(3x^2)$ (B). $3x^2 \cos(x^3)$ (C). $3 \sin^2 x$ (D). $\sin(3x^2)$ (E). none of above

10. If $f(x) + x^2[f(x)]^3 = 10$, and $f(1) = 2$, find $f'(1)$.

Select the correct answer.

- (A). $-\frac{16}{13}$ (B). $-\frac{6}{13}$ (C). $\frac{16}{13}$ (D). $\frac{6}{13}$ (E). none of above

11. $\int \cos(3x) dx = ?$

Select the correct answer.

- (A). $\sin(3x) + C$ (B). $3 \sin(3x) + C$ (C). $\frac{1}{3} \sin(3x) + C$

- (D). $3 \sin(x) + C$ (E). none of above

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12. $\int_0^2 |x-1| dx = ?$

Select the correct answer.

- (A). 0 (B). 1 (C). 2 (D). 3 (E). none of above

13. $\int_1^2 x\sqrt{x-1} dx = ?$

Select the correct answer.

- (A). $\frac{16}{15}$ (B). $\frac{15}{16}$ (C). $\frac{2}{3}$ (D). $\frac{3}{2}$ (E). none of above

14. Find the absolute maximum value of the function $f(x) = \sqrt{x} - \frac{1}{3}x$ on $0 \leq x \leq 9$.

Select the correct answer.

- (A). $\frac{9}{4}$ (B). $\frac{3}{4}$ (C). $\frac{4}{3}$ (D). 0 (E). none of above

15. A region bounded by the curves : $y = x$, $y = 0$ and $x = 1$, find the volume of the region rotates about x-axis.

Select the correct answer.

- (A). π (B). $\frac{\pi}{2}$ (C). $\frac{\pi}{3}$ (D). $\frac{\pi}{4}$ (E). none of above

※Multiple Choice (16~20, 5% each) (每題至少有二正確選項，完全答對得 5 分，

其餘情形得 0 分)

16. Consider the function $f(x) = |\sin x|$.

Select the correct statements.

(A). $f(x) \geq 0$ for every $x \in (-\infty, \infty)$.

(B). $f(x)$ is continuous on $(-\infty, \infty)$.

(C). $f(x)$ is differentiable on $(-\infty, \infty)$.

(D). $\lim_{x \rightarrow \infty} f(x)$ does not exist.

(E). $\int_a^b f(x) dx$ does not exist for $-\infty < a < b < \infty$.

17. Let $f(x)$ and $g(x)$ be two integrable and differentiable functions with $f(x) \geq g(x)$ on \mathcal{R} . Which of the following statements are true?

(A). $f'(x) - g'(x) \geq 0, x \in \mathcal{R}$.

(B). $|f(x)| \geq |g(x)|, x \in \mathcal{R}$.

(C). $f^2(x) \geq g^2(x), x \in \mathcal{R}$.

(D). $f'(x) \geq g'(x), x \in \mathcal{R}$.

(E). $\int_a^b f(x) dx \geq \int_a^b g(x) dx$, where $a < b$.

18. Which of the following statements are true?

(A). If $f(x)$ is continuous on \mathcal{R} , then it is differentiable on \mathcal{R} .

(B). If $f(x)$ is differentiable on \mathcal{R} , then it is continuous on \mathcal{R} .

(C). If $f(x)$ is continuous on \mathcal{R} , then $\int_a^b f(x) dx$ exists for $-\infty < a < b < \infty$.

(D). If $\int_a^b f(x) dx$ exists for every $-\infty < a < b < \infty$, then $f(x)$ is continuous on \mathcal{R} .

(E). If $\int_a^b f(x) dx$ exists for every $-\infty < a < b < \infty$, then $f(x)$ is differentiable on \mathcal{R} .

19. The position of a partical is given by $s = f(t) = t^3 - 6t^2 + 9t$, where t is measured in seconds and s in meters.

Which of the following statements are correct?

(A). The velocity after 2 s is -3 m/s.

(B). The partical is at rest after 1 s and 3 s.

(C). The total distance traveled by the partical during the first second is 10 m.

(D). The acceleration after 2 s is 0 m/s^2 .

(E). The average velocity during the first 4 s is 1 m/s.

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20. Which of the following functions have an inverse function?

(A). $f(x) = \sin x, \quad x \in [-\pi, \pi]$.

(B). $f(x) = \sin x, \quad x \in \left[-\frac{\pi}{2}, \frac{\pi}{2}\right]$.

(C). $f(x) = \cos x, \quad x \in [-\pi, \pi]$.

(D). $f(x) = \cos x, \quad x \in \left[-\frac{\pi}{2}, \frac{\pi}{2}\right]$.

(E). $f(x) = x, \quad x \in [-1, 1]$.